

# High-resolution data-driven models of Daylight Redirection Components

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## Abstract

*Daylight Redirecting Components (DRCs) guide daylight to zones with insufficient daylight exposure. They reduce energy demand for lighting, heating and cooling, and improve visual and thermal comfort. The data-driven model in Radiance is a means to model DRCs in daylight simulation. Rather than internal optical mechanisms, their resulting Bidirectional Scattering Distribution Function (BSDF) is replicated.*

*We present models of two DRCs that are generated from measurements. The impact of the following three necessary steps in the generation of data-driven models from measured BSDF shall be evaluated:*

- 1) interpolation between measurements at sparse sets of incident directions;*
- 2) extrapolation for directions that cannot be measured;*
- 3) application of a directional basis of given directional resolution.*

*It is shown that data-driven models can provide a realistic representation of both DRCs. The sensitivity to effects from interpolation differs for the two DRCs due to the varying complexity of their BSDFs. Due to the irregularity of the measured BSDFs, extrapolation is not reliable and fails for both tested DRCs. Different measurement and modeling protocols should be applied to different class systems, rather than aiming at a common low-resolution discretization.*

## Keywords

*daylight simulation, data-driven model, BSDF, Radiance*

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# 1 INTRODUCTION

A Daylight Redirecting Component (DRC) controls the admission and directional distribution of daylight in buildings. The application of a DRC aims to optimize the utilization of daylight for visual and thermal comfort, well-being and energy efficiency (Gago, Muneer, Knez, & Köster, 2015; Hoffmann et al., 2016). Typical applications of DRCs include the upward deflection of daylight transmitted through the facade to achieve even illumination, or the directional selective transmission only of diffused daylight through horizontal glazing (Ruck et al., 2000; Nair, Ramamurthy, & Ganesan, 2014). Deflection and directional selectivity are some examples of the irregular optical properties of DRCs that can be utilized for optimized daylight performance, but are beyond the capabilities of typical simulation tools employed in building design (Ward & Shakespeare, 1998). To address this lack of predictability as a barrier for the widespread and successful application of the technique, different modeling approaches have been demonstrated for the application in daylight simulation.

Software algorithms such as forward ray-tracing or the bidirectional combination of backward ray-tracing and forward photon-mapping can replicate the light propagation through DRCs based on geometric models. Photon mapping has been implemented in the daylight simulation software Radiance (Noback, Grobe, & Wittkopf, 2016; Schregle, Bauer, Grobe, & Wittkopf, 2015; Schregle, Grobe, & Wittkopf, 2016) and was extended to support even advanced simulation techniques such as Climate-Based Daylight Modeling (CBDM). However, this explicit approach demands highly detailed simulation models in cases where the micro-structures in the scale of millimeters comprising DRCs covering entire building facades shall be modeled geometrically.

Models of the Bidirectional Scattering Distribution Function (BSDF) replicate the effective light scattering characteristics of DRCs rather than the comprised geometric structures causing it. Such models describe light propagation as a function of incident and outgoing light direction through a surface. The two directions, relative to a coordinate system attached to the surface of the DRC, are typically expressed as pairs of elevation and azimuth angles  $\theta, \phi$ . The BSDF approximates light scattering as a uniform, average property of a thin surface. Analytic models of the BSDF of the DRCs have been developed and validated (Greenup, Edmonds, & Compagnon, 2000; Maamari et al., 2006; Laouadi & Parekh, 2007). However, the development of such custom models for particular devices and applications is elaborate and has limited scope for generalization.

A general approach is the use of data-driven models of the BSDF. Such models comprise a discrete set of luminous coefficients, evaluating the light propagation through the device for incident and outgoing directions merged into regions according to a given directional basis. They can be generated by computational simulation as well as from measurements (Mohanty Yang, & Wittkopf, 2012; McNeil, Lee, & Jonsson, 2017). As a "black box", data-driven models hide the complexity of the internal optical mechanisms effecting light propagation through the device from simulations employing the model (Kuhn, Herkel, Frontini, Strachan, & Kokogiannakis, 2011; Appelfeld, McNeil, & Svendsen, 2012). A symmetric directional basis of 145 incident and 145 outgoing directions is in widespread use and supported by a set of software tools mainly developed by Lawrence Berkeley National Laboratory (LBNL), such as Radiance and Window. The latter allows the combination of the BSDFs of co-planar fenestration layers into that of an entire glazing assembly, and provides an interface for the Complex Glazing Database. The directional basis is employed in multiple domains of building simulation and backs advanced CBDM methods such as the three-phase method (Klems, 2013; McNeil & Lee, 2013). An asymmetric directional basis of 145 incident and 1297 outgoing directions was recommended by the International Energy Agency (IEA) and can be employed to pre-compute transmission through DRCs with mkillum in Radiance (de Boer, 2005; Kämpf & Scartezzini, 2011).

The highest directional resolution can be achieved by the locally adaptive tensor-tree format of Radiance, allowing up to 16,384 incident and 16,384 outgoing directions. To be applicable in simulation, and to allow sharing and re-use such as in model libraries, a compact representation for the data-driven model is required. Starting from a four-dimensional tensor of initially constant directional resolution, a data-reduction algorithm selectively merges cells representing adjacent directions with little variance in the BSDF to generate the compact tensor-tree (Ward, Mistrick, Lee, McNeil, & Jonsson, 2011; Ward, Kurt, & Boneel, 2012). The combination of the optical properties of fenestration layers described by the tensor-tree format has been demonstrated as a reflection of the method implemented in Window (Grobe, 2017).

The use of discrete data to describe the continuous BSDF introduces problems of resolution into the generation, storing and application of models. Measurements sample the BSDF for a finite set of incident and outgoing directions. This set of directions is bound to the geometric constraints of the instrument, excluding, for example, directions close to grazing and retro-reflection (Krehel, Grobe, & Wittkopf, 2017). While their underlying dataset is incomplete by necessity, models must provide coefficients for any pair of directions, and therefore rely on interpolation and extrapolation. Data-reduction such as the merging of directions leads to a loss of information in the model.

In this research, the impact of both the interpolation and extrapolation in the generation of models from measurements, and the effect of directional resolution and data-reduction applied to the data-driven model shall be assessed for two exemplary DRCs.

A better understanding of the parameters defining measurement and model generation will guide the generation and application of data-driven BSDF models. Such models would provide a general means to better predict the daylight performance of DRCs in buildings, supporting both practitioners and researchers in the field of daylighting.

## 2 METHODOLOGY

### 2.1 TWO CASES OF DAYLIGHT REDIRECTING COMPONENTS

The selected case studies focus on typical examples of shading and non-shading DRCs for applications in vertical and horizontal glazing. The examples employ the optical mechanisms of reflection and refraction on periodic structures. Due to the small size of these structures, their scattering properties are perceived as uniform when seen from the position of a typical observer. It is therefore possible to model both DRCs by their effective BSDFs rather than explicit modeling of the geometrical structures causing their irregular transmission characteristics.



FIG. 1  $DRC_1$  deflecting sunlight upward

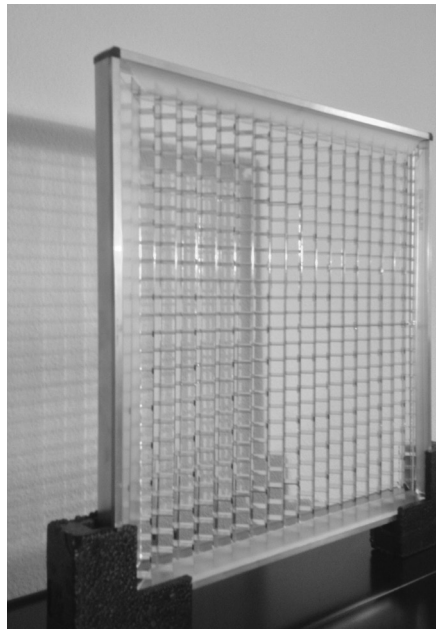


FIG. 2  $DRC_2$  controlling direct transmission.

$DRC_1$  (Fig. 1) is a glazing unit with applied films. A prismatic film is laminated on the inward-facing surface of an outer pane and deflects incident light. A diffusing film is applied to the inner pane to achieve smooth light distribution. The system improves daylight supply by deflection but provides no shading effects (Kazanasmaz, Grobe, Bauer, Krehel, & Wittkopf, 2016; McNeil et al., 2016). It can be employed e.g. in the upper zone of windows. The exact geometry of the micro-structures on both films is not known. The utilization of a data-driven model, based on measured BSDF data, allows the replication of its transmission characteristics even without detailed knowledge of the system's composition.

$DRC_2$  (Fig. 2), a grid of tilted anidolic light-shafts, reflects direct sunlight but transmits and evenly distributes diffuse skylight. It can control solar gains and glare when applied to skylights. The geometry of its highly reflective structure is shown in detail by Grobe et al. (2015).

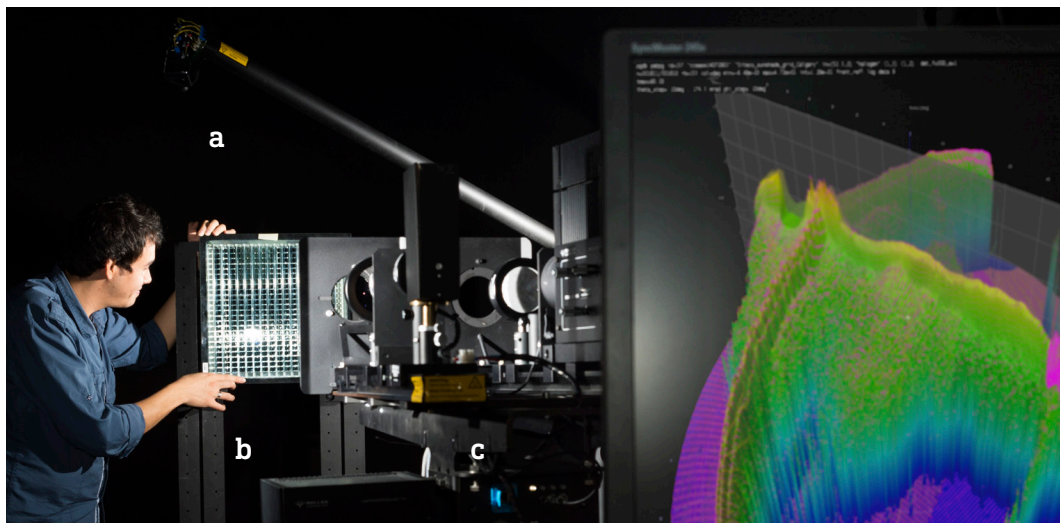


FIG. 3 Gonio-photometer, comprising detector (a) moving around rotatable sample (b), and illuminator (c).

## 2.2 MEASUREMENT

The BSDFs of the DRCs are measured on a scanning gonio-photometer as shown in Fig. 3. The characterization of each DRC comprises measurements of the illuminator's intensity distribution followed by the recording of light scatter for each given incident direction. The incident direction is set by rotation of the sample, and the detector subsequently performs a continuous scan around the sampling aperture while recording illuminance  $E_s$ . The scan path is adaptive to the measurement and allows refinement e.g. for regions where transmission peaks occur.

Due to the prior beam characterization, the BSDF can be computed without photometric calibration from  $E_s$ , the power of the incident beam  $P_i$  (the integration of the unobstructed measurement) and the cosine of the outgoing elevation angle  $\theta_s$ :  $BSDF = E_s \times P_i^{-1} \times \cos(\theta_s)^{-1}$  (Apian-Bennewitz, 2010).

The fine structures of  $DRC_1$  allow to focus of the illuminator on the detector for maximum directional resolution. The BSDF of  $DRC_2$  is measured under collimated illumination, leading to a widened illuminated sampling aperture covering a representative number of periodical structures.

An asymmetric resolution of coarse incident directions  $\theta_i, \varphi_i$  and dense outgoing scattered light directions  $\theta_s, \varphi_s$  is chosen, assuming that features in the BSDFs require dense sampling of outgoing directions, but change only gradually between adjacent incident directions. Due to the symmetry of both DRCs, incident azimuth angles are varied as  $\varphi_i = 0^\circ$  to  $180^\circ$ . For  $DRC_1$ ,  $\varphi = 0^\circ$  corresponds to up, for  $DRC_2$  to North in typical applications.

Three sets of incident directions are distinguished (Fig. 4):

- *Coarse* (black): Low resolution with  $\theta_i = 10^\circ$  to  $50^\circ$  in increments of  $20^\circ$ ,  $\varphi_i = 0^\circ$  to  $180^\circ$  in increments of  $30^\circ$ .
- *Refined* (green): Refining *Coarse* with  $\theta_i = 0^\circ$  to  $60^\circ$  in increments of  $10^\circ$ ,  $\varphi_i = 0^\circ$  to  $180^\circ$  in increments of  $15^\circ$ .
- *High* (blue): Complementing *Coarse* and *Refined*, this dataset comprises incident elevation angles above  $60^\circ$ .

To test interpolation and extrapolation, the BSDFs for two additional incident directions T1  $\theta_i = 40^\circ$ ,  $\varphi_i = 30^\circ$  and T2  $\theta_i = 70^\circ$ ,  $\varphi_i = 30^\circ$  (red) are measured. In the results, these directions are shown mirrored as red circles.

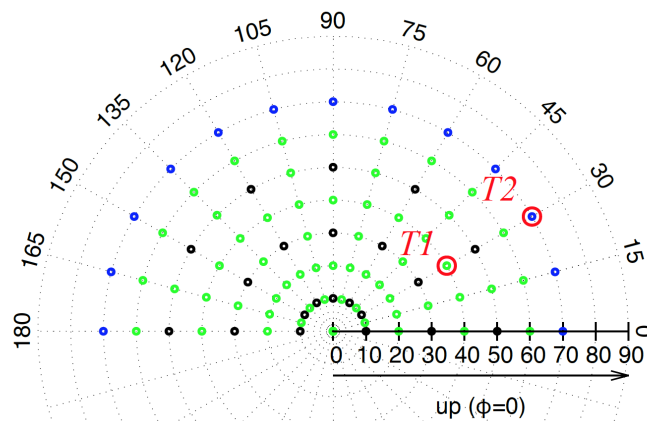


FIG. 4 Incident directions *Coarse* (black), *Refined* (green), *High* (blue), T1 and T2 (red).

## 2.3 MODEL GENERATION

Three data-driven models are generated from the three datasets. The process comprises three passes:

- *pabopto2bsdf* fits a set of radial basis functions as interpolants to the four components (reflection front/back and transmission front/back) of the measurement.
- These interpolants are subsequently sampled by the command *bsdf2tree*<sup>4</sup> into a four-dimensional tensor of  $2^{4 \times 7} = 268,435,456$  elements. Higher resolutions are not possible on typical hardware due to memory constraints.
- *bsdf2tree* internally calls *rtree\_reduce* to reduce this vast amount of data by merging adjacent directions of low local variance until 90% of the initial dataset is eliminated, and saves the resulting tensor tree into a XML-formatted file.

The method provides a set of three BSDF-models of adaptive resolution for each DRC.

- $M1_{DRC1}$ ,  $M1_{DRC2}$  comprise BSDF from *Coarse*.
- $M2_{DRC1}$ ,  $M2_{DRC2}$  comprise datasets *Coarse* and *Refined*.
- $M3_{DRC1}$ ,  $M3_{DRC2}$  comprise *Coarse*, *Refined* and *High*.

## 2.4 COMPARISON OF TRANSMISSION DISTRIBUTIONS

To evaluate the effect of parameters in the measurement and model-generation, pairs of the BSDF for a given direction are compared. We evaluate only transmission to the interior, which is of particular importance in building applications.

To maintain readability up to high outgoing directions, the Differential Scattering Function (DSF), equal to  $\text{BSDF}(\theta_i, \varphi_i, \theta_s, \varphi_s) \cos(\theta_s)$ , is plotted, rather than the BSDF. The latter, due to the division by  $\cos(\theta_s)$ , tends to exaggerate data at measurement points close to grazing. The transmission distributions are plotted in polar coordinates, the center being  $\theta = 180^\circ$  and  $\varphi = 0^\circ$  aiming right.

## 2.5 EVALUATION OF THE EFFECTS OF INTERPOLATION AND EXTRAPOLATION

The BSDFs of both DRCs for direction *T1*, as predicted by *M1* and *M2*, are compared to the measurements. Predictions by *M1* are results of interpolation, while *M2* rely on measured data.

The measured BSDFs of *DRC<sub>1</sub>* and *DRC<sub>2</sub>* for *T2* are compared to the extrapolated BSDFs from *M2* and *M3*. As no data for incident directions above  $\theta_i = 60^\circ$  is employed in the generation of *M2*, these models provide results based on extrapolation. *M3* comprises measured data for the queried incident direction.



# EVALUATION OF THE EFFECTS OF RESOLUTION AND DATA-REDUCTION

For both DRCs, variants of  $M3$  of reduced resolution (tensor of  $2^{4 \times 6} = 16,777,216$  elements representing  $2^{6 \times 2}$  incident and  $2^{6 \times 2}$  outgoing directions) without data-reduction are generated. These are compared to variants of high resolution ( $2^{7 \times 2}$  incident and  $2^{7 \times 2}$  outgoing directions), but with a data-reduction of 97% applied, leading to comparable model sizes.

## 3 RESULTS AND DISCUSSION

### 3.1 MEASUREMENT

Fig. 5 and Fig. 6 show the DSF of  $DRC_1$  and  $DRC_2$  measured for  $T1$  and  $T2$ . The prismatic structure of  $DRC_1$  spreads the scattered light to a rim with an upward peak for  $T1$ .  $DRC_2$  shows two forward peaks for  $T1$  and a pattern of scattered light on the opposite side of the  $\varphi_i = 0^\circ, 180^\circ$  plane. These peaks disappear towards the  $T2$  direction with a remaining distribution of diffused light.

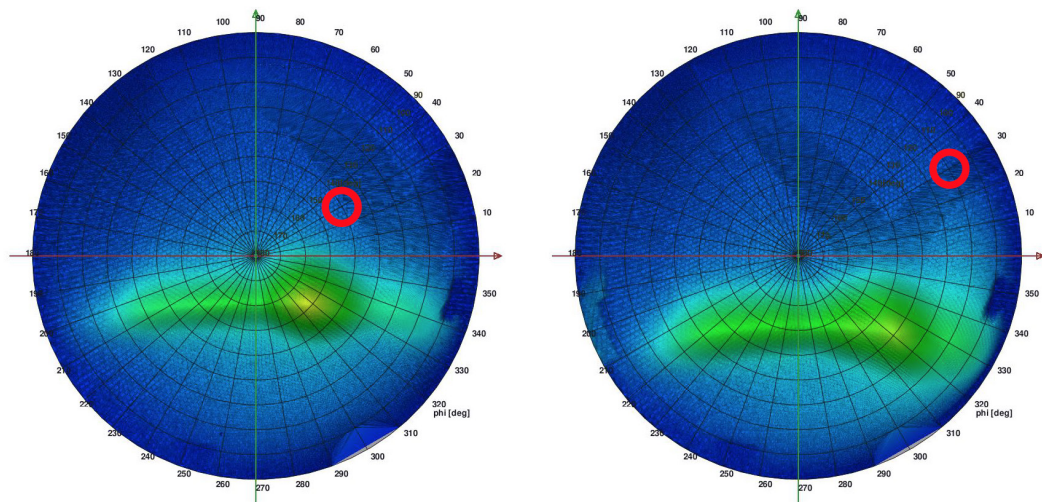


FIG. 5 Measurement: DSFs of  $DRC_1$  for incident direction  $T1$  (left, red) and  $T2$  (right, red).

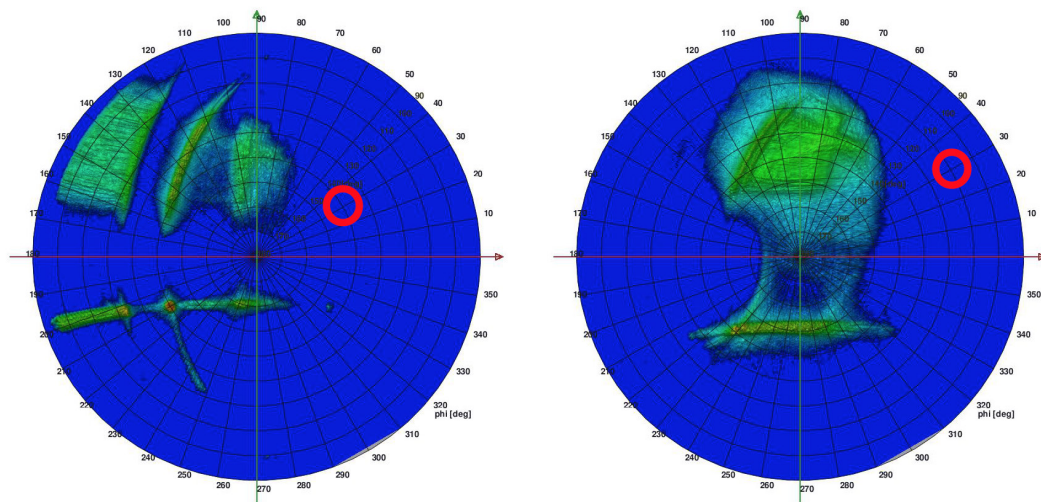


FIG. 6 Measurement: DSFs of  $DRC_2$  for incident direction  $T1$  (left, red) and  $T2$  (right, red).

### 3.2 INTERPOLATION EFFECTS

$M1$  and  $M2$  lead to almost identical results for  $DRC_1$  but do not show the ridge as pronounced measurements. Transmission to the downward direction (lower left quadrant) is underestimated by  $M1$  when compared to  $M2$  (Fig. 7).

For  $DRC_2$ ,  $M1$  replicates the configuration of features found in the measurement, such as a strong peak due to direct transmission at  $\theta_s = 140^\circ$ ,  $\varphi_s = 210^\circ$  (Fig. 8). The shape of other features, such as a secondary peak at  $\theta_s = 120^\circ$ ,  $\varphi_s = 200^\circ$  and two parallel rims in the upper half of the plot, are not maintained by  $M1$ , but  $M2$ . The latter only differs from the measurement by the less pronounced contours of its features, and a gradient toward grazing for which no measured data exists.

The interpolation by  $M1$  replicates the characteristic upward deflection of  $DRC_1$  as well as the distinct features of  $DRC_2$ . The underestimation of downward transmission through  $DRC_1$  may however effect results in daylight simulation.

### 3.3 EXTRAPOLATION EFFECTS

As shown in Fig. 9, the extrapolated DSF of  $DRC_1$  for  $T2$  from  $M2$  is almost flat in the deflected upward direction and lacks any peaks, which are present in the result from  $M3$ . Model  $M2$  does not replicate the characteristic deflection of light toward the ceiling for high incident elevation directions, if these are not within the boundaries of the measurement.



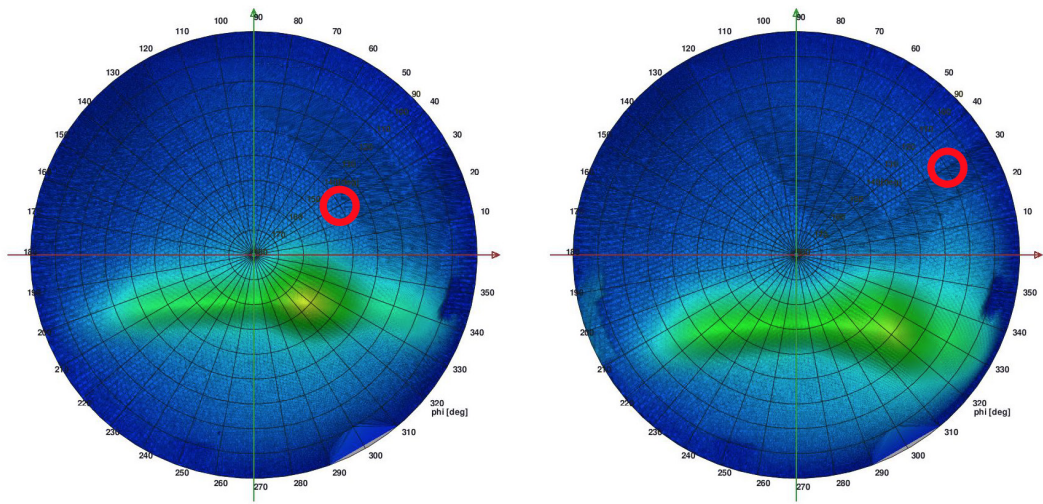


FIG. 7 Predicted DSF of  $DRC_1$  for incident direction  $T1$  (red) from interpolated  $M1$  (left) and measured  $M2$  (right).

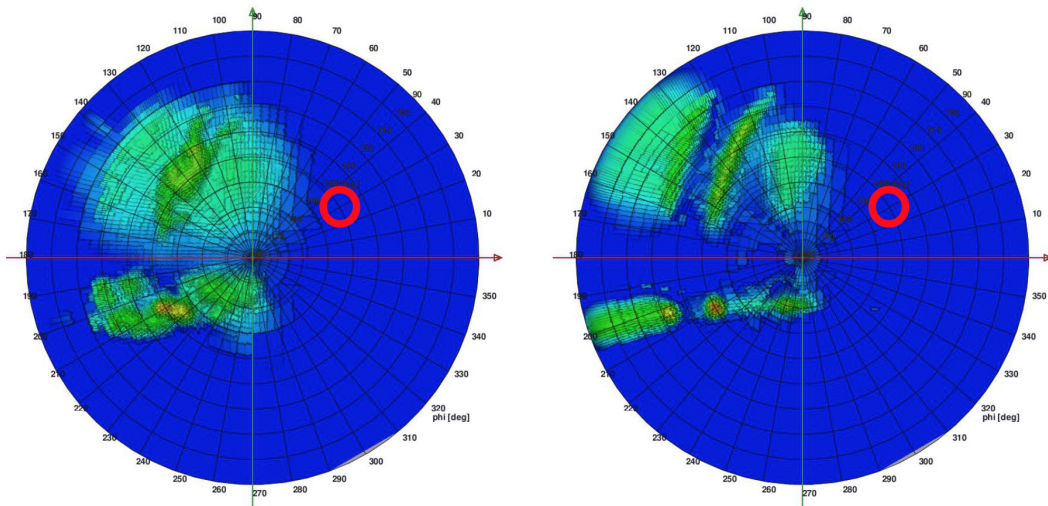


FIG. 8 Predicted DSF of  $DRC_2$  for incident direction  $T1$  (red) from interpolation  $M1$  (left) and measurement  $M2$  (right).

As no diffused background is present in the DSF of  $DRC_2$ , and no peaks in the complex DFS for  $T2$  are extrapolated,  $M2$  indicates almost zero transmission. This is contradicted by  $M3$  (Fig. 10), which closely matches the measured distribution. Due to the typical horizontal installation of  $DRC_2$ , this corresponds to a significant underestimation of low sun angles e.g. in the morning and afternoon, if the boundaries of the measurement are not extended.

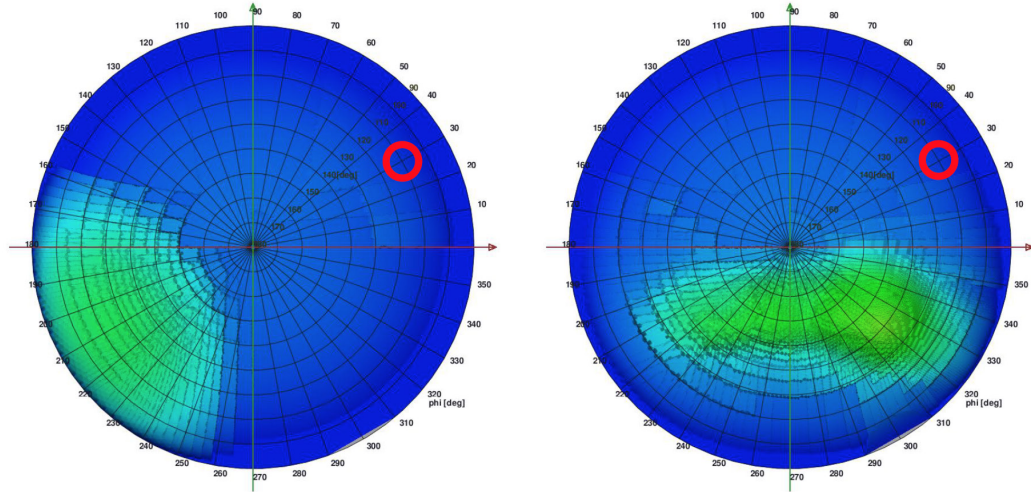


FIG. 9 Predicted DSF of  $DRC_1$  for incident direction  $T2$  (red) from extrapolation  $M2$  (left) and measurement  $M3$  (right)

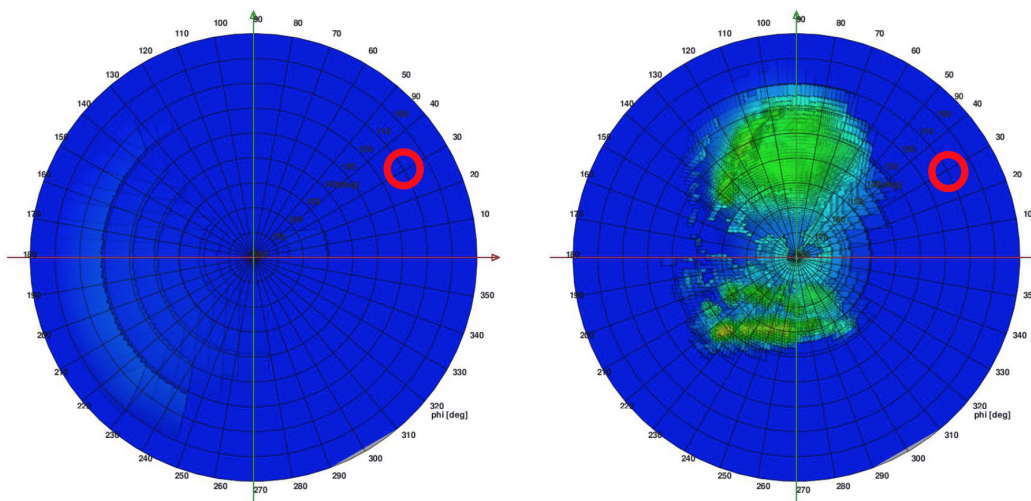


FIG. 10 Predicted DSF of  $DRC_2$  for incident direction  $T2$  (red) from extrapolation  $M2$  (left) and measurement  $M3$  (right)

### 3.4 EFFECTS OF RESOLUTION AND DATA-REDUCTION

Fig. 11 and Fig. 12 show the DSFs for  $DRC_1$  and  $DRC_2$  at incident direction  $T1$  at resolution  $k = 6$  without, and  $k = 7$  with 97% data-reduction applied. While the latter can better resolve the forward peak of  $DRC_2$  (Fig. 12, right) data-reduction does not affect any important features for the two DRCs.

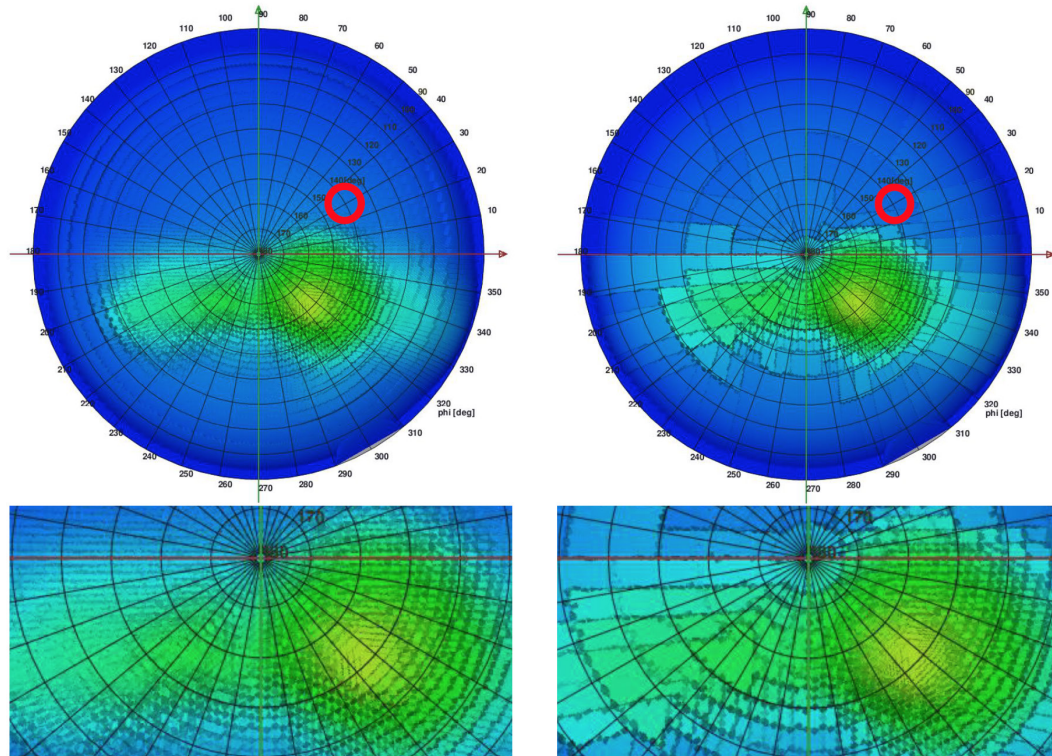


FIG. 11 DSF of  $DRC_1$  for direction  $T1$  (red). Left: Resolution  $k=6$ , no data-reduction. Right:  $k=7$ , data-reduction by  $pt=97\%$ .



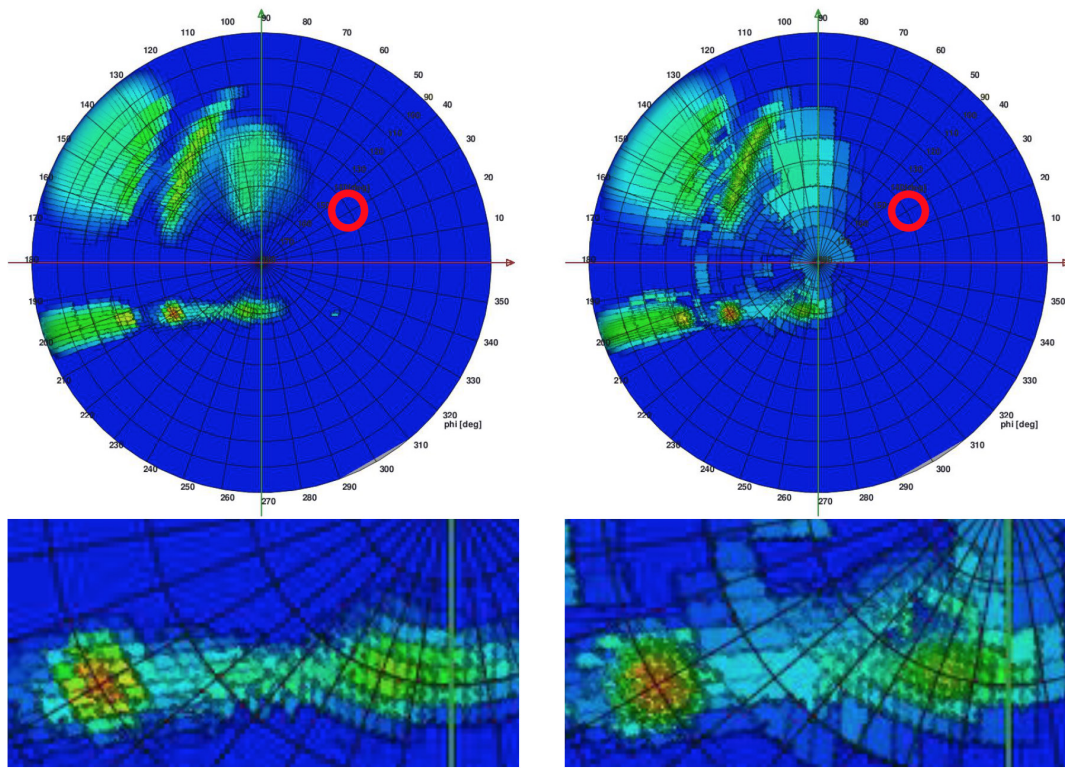


FIG. 12 DSF of  $DRC_2$  for direction  $T1$  (red). Left: Resolution  $k=6$ , no data-reduction. Right:  $k=7$ , data-reduction by  $pt=97\%$ .

### 3.5 CONCLUSIONS AND OUTLOOK

Data-driven models of two exemplary, micro-structured DRCs were generated based on measurements of their BSDF employing a gonio-photometer. The tensor-tree format of Radiance was employed, as it provides a generic means to model the irregular optical properties characterizing DRCs based on computation or measurement. Resulting models can be applied directly in daylight simulations with Radiance, or can be efficiently combined with BSDF of other clear or non-scattering fenestration layers using an extended matrix formalism. The influence of interpolation and extrapolation, depending on the density of measurements as input for the model generation, was evaluated, along with the impact of model output parameters such as directional resolution and data-reduction.

While the data-driven model in Radiance is found to be capable of modeling the irregular BSDFs of both  $DRC_1$  and  $DRC_2$  by interpolation, less pronounced peaks such as the downward transmission through  $DRC_1$  may be underestimated. Resolution of measured incident directions is of particular importance for DRCs that abruptly change their properties between incident directions, such as  $DRC_2$ , if details of the complex BSDF are to be maintained.

Extrapolation for a complex BSDF, as a characteristic of DRC, was not reliable, and did not lead to valid results for either of the assessed samples. Consequently, models must be utilized only within the boundaries of measurements employed in model generation. Computational simulation to complement measurements even up to grazing have been demonstrated (Krehe, l) but require detailed prior knowledge about the geometry and surface properties of DRCs. The extension of the geometrical boundaries to higher incident elevation angles poses a challenge. The sampling aperture illuminated by a beam of circular diameter chosen to cover a representative amount of periodical

features of a given DRC at normal incident tends to exceed the sample size at high elevation angles. While this can be addressed, for example by shaping the beam employing elliptical or slit baffles, the resulting loss of beam power affects the signal to noise ratio of the measurement.

Data-reduction merges contiguous directions of low variance. This allows locally high resolution, e.g. of distinct peaks at comparable file sizes, but effects less pronounced features such as ridges in the BSDF of  $DRC_2$ .

The sensitivity of model accuracy to directional resolution and data-reduction depends on the complexity of the BSDF, and shall be further studied for different classes of DRCs. Efficient configurations of the illuminator are currently being investigated to limit the sampling aperture to the sample size even at very high incident directions.

The tensor-tree format and the routines for interpolation of measured BSDF implemented in Radiance provide a means to model DRCs characterized by high directional selectivity and highly directional, irregular transmission. Its variable resolution promises higher accuracy in daylight simulation compared to the commonly used BSDF models of low directional resolution. In order to guide model generation and application employing the tensor-tree, a better understanding of the impact of directional resolution on assessments of different aspects of daylight performance, such as daylight supply, glare and energy-efficiency, is required.

## Endnotes

1. The command line parameters for `bsdf2ttree` are `-t4 -g 7 -t 90` for a four-dimensional tensor of initial directional resolution  $2^{4 \times 7}$ . The target for the data reduction is 90%.
2. `bsdf2ttree` called with parameters `-t4 -g 6 -t -1`.
3. `bsdf2ttree` called with parameters `-t4 -g 7 -t 97`.

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